



CIPANP 2012

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# Measurements of the Top Quark Charge Asymmetry at CDF

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# Outline

- A little about the Top Quark at the Tevatron
  - *What is  $A_{FB}$ ? How we measure it and why we care*
  - Standard Model Predictions
- Reconstructing tops/anti-tops and "Raw" Measurements of  $A_{FB}$  in both Lepton+Jets and Dilepton events
  - Raw Asymmetry results
- Checks: *"Is it real? Should I take this seriously?"*
- Going beyond the Raw measurement: *"What do inquiring Minds Want to Know?"*
  - Corrected  $A_{FB}$
  - Differential Measurements of  $A_{FB}$
- Summary and Conclusions

## CDF Public Notes

- CDFNote 10436: Dileptons
- CDFNote 10774: Lepton+Jets
- CDFNote 10807: Differential Measurements

# Top Quark and the Tevatron

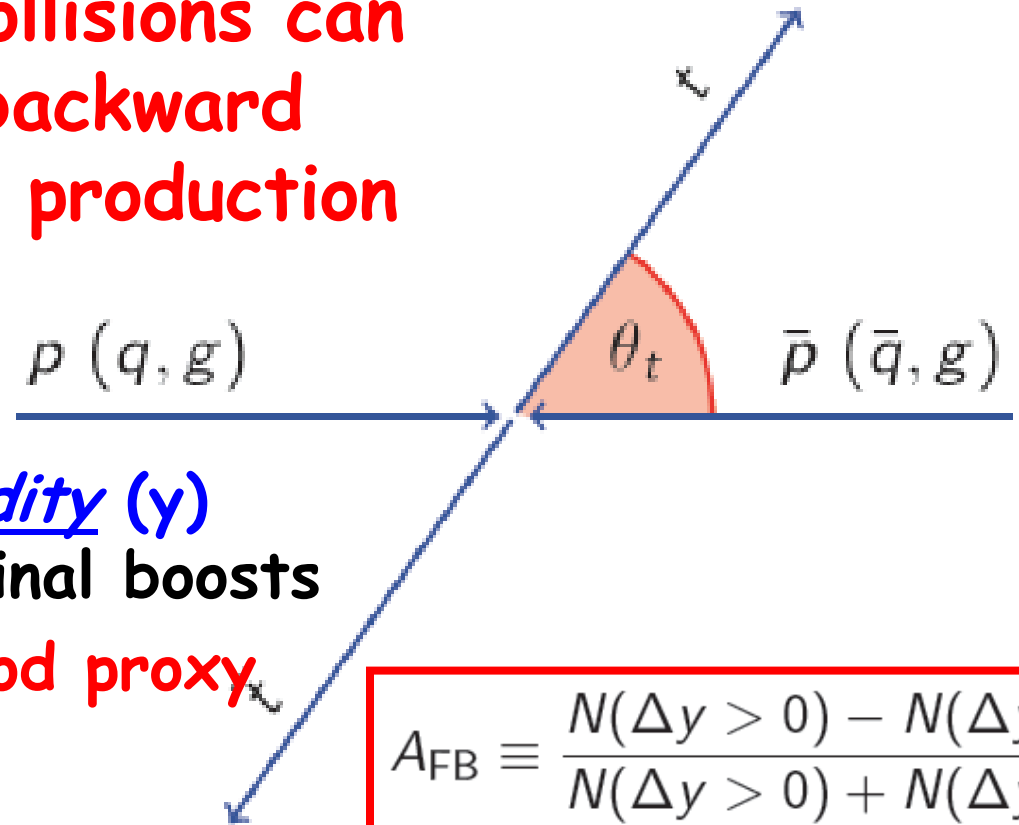
- *“Just the facts Ma’am”*
- Heaviest of the known particles
  - Mass  $\approx 172.5 \text{ GeV}/c^2$
- Considering top quark pairs produced at the Fermilab Tevatron
  - $\sqrt{s} = 1.96 \text{ TeV}$
  - Just completed its data taking phase
  - Collected  $8.7 \text{ fb}^{-1}$  of data useful for these analyses
  - Cross section  $\approx 7.5 \text{ pb}$ 
    - Total of about 65k produced
    - Identify and study about 3,000

# First things first...

- *What is  $A_{FB}$ ?*
- *How do we measure  $A_{FB}$ ?*
- *Why do we care?*
  - Standard Model Predictions
  - Possible New Physics Models

# What are $A_{FB}$ and $\Delta Y$ ?

In proton-antiproton collisions can measure the forward-backward asymmetry ( $A_{FB}$ ) in the production angle



Transform from  $\Theta_t$  to rapidity ( $y$ )

Invariant under longitudinal boosts

Rapidity difference is a good proxy for production angle

$$A_{FB} \equiv \frac{N(\Delta y > 0) - N(\Delta y < 0)}{N(\Delta y > 0) + N(\Delta y < 0)}$$

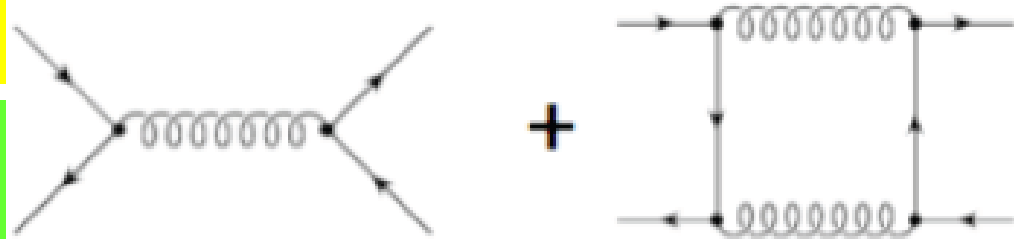
Measure  $\Delta y = y_t - y_{\bar{t}}$ , where  $y = \frac{1}{2} \ln\left(\frac{E + p_z}{E - p_z}\right)$

Note:  $y$  doesn't have the usual geometric angle many of us are used to.  
At hadron colliders we usually use pseudo-rapidity which assumes  $m=0$   
→ Here  $E$  and  $p$  not close to equal because of the top mass

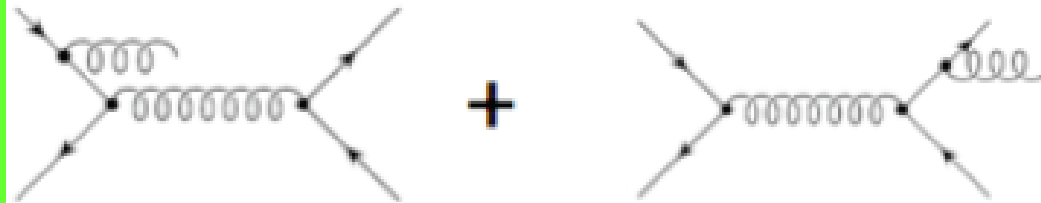
# $A_{FB}$ in the Standard Model

- Standard Model has no asymmetry at LO
- NLO has interference terms that give a small asymmetry
- Some uncertainty regarding theory predictions
  - Use POWHEG central value and a 26% correction for EWK contributions

Born + Box Interference  
Positive Contribution to  $A_{FB}$



ISR/FSR Interference  
Negative Contribution to  $A_{FB}$



$$A_{FB}^{NLO} = 6.6\%$$

*POWHEG*: JHEP 0709, 126 (2007)

*EW Corrections*: Phys. Rev. D 84, 093003 (2011); JHEP 1201, 063 (2012); arXiv:1201.3926[hep-ph]

# Examples of New Physics That could give a Large $A_{FB}$

Two main classes of models

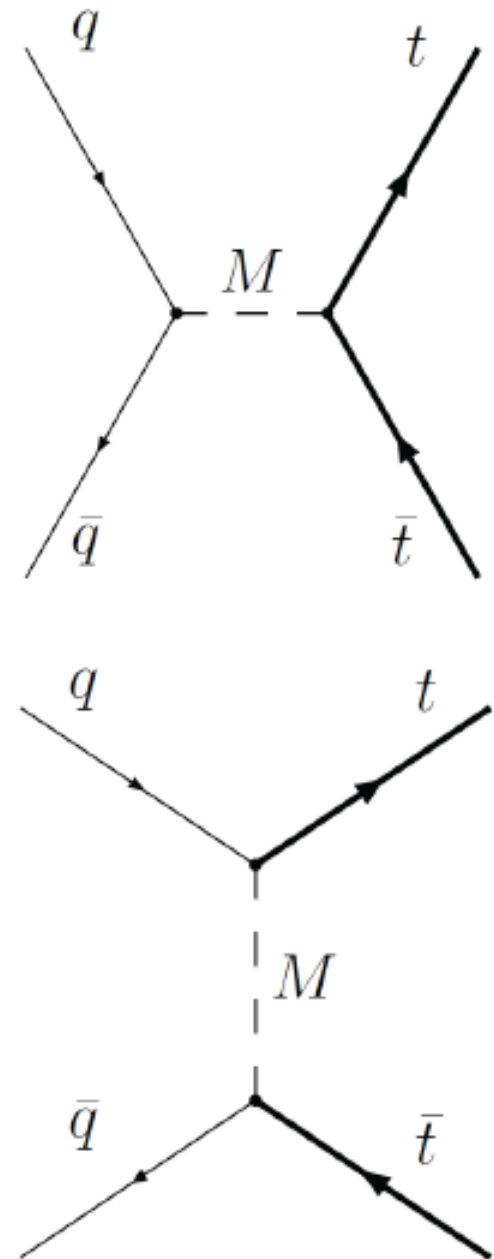
- S-channel mediator
  - e.g. axigluon
- T-channel flavor changing mediator
  - e.g.  $W'$  or  $Z'$

Although many of these have strong constraints, they provide a good model for searches

For a review see:

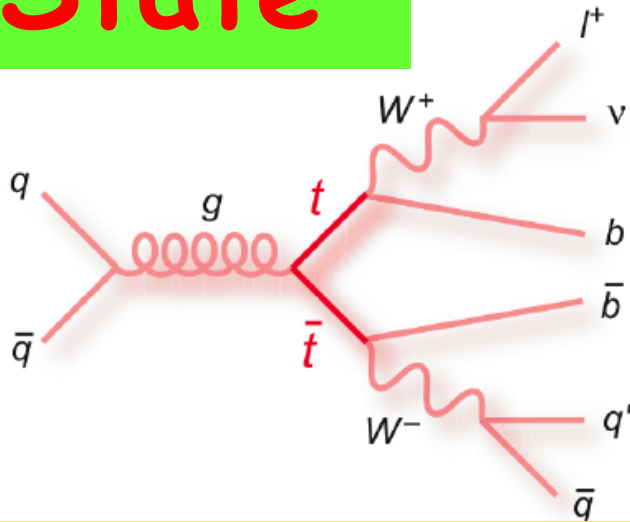
M. Gresham, I.-W. Kim and K. Zurek,

*Phys. Rev. D*83 114027 (2011)



# Selecting Top Quark Events

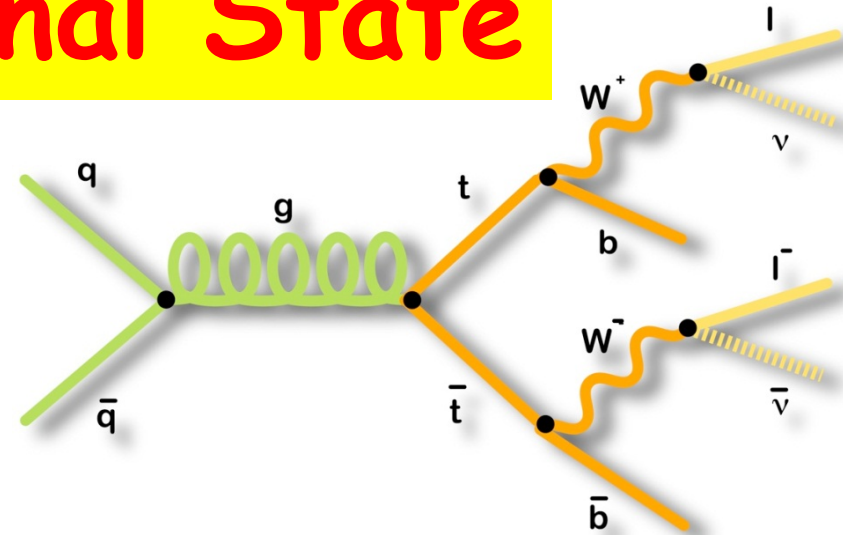
## Lepton+Jets Final State



- 1 reconstructed lepton
- Missing transverse energy
- $\geq 4$  jets (1 *b*-tag)
- $\Sigma E_T > 220 \text{ GeV}$

Bigger branching fraction, more final state particles to measure, bigger backgrounds

## Dilepton Final State



- 2 reconstructed leptons
- Missing transverse energy
- $\geq 2$  jets
- $\Sigma E_T > 200 \text{ GeV}$
- Higher purity sample, but smaller branching fraction, two leptons have better angles, but two neutrinos cause reconstruction ambiguities



# Events Observed and Expected from Backgrounds

Lepton+Jets

$8.7 \text{ fb}^{-1}$

Source	Predicted Event Count, $8.7 \text{ fb}^{-1}$
W + Heavy Flavor	$241 \pm 78$
Non-W (QCD)	$98 \pm 51$
W + Light Flavor	$96 \pm 29$
Single Top	$33 \pm 2$
Diboson	$19 \pm 3$
Z + Jets	$18 \pm 2$
Total Background	$505 \pm 123$
Top Pairs (7.4 pb)	$2037 \pm 277$
Total Prediction	$2542 \pm 303$
Data	2498

Dilepton

$5.1 \text{ fb}^{-1}$

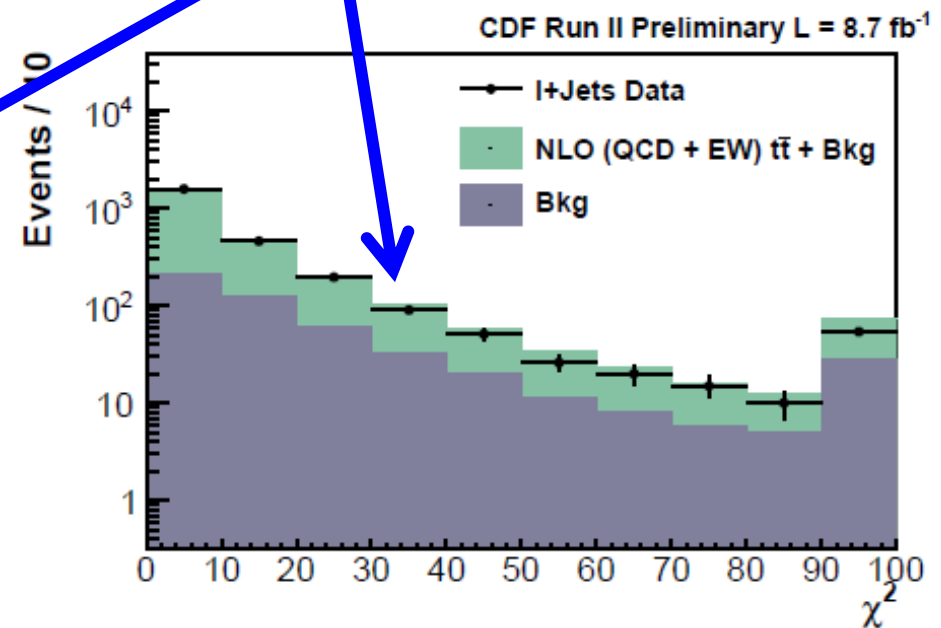
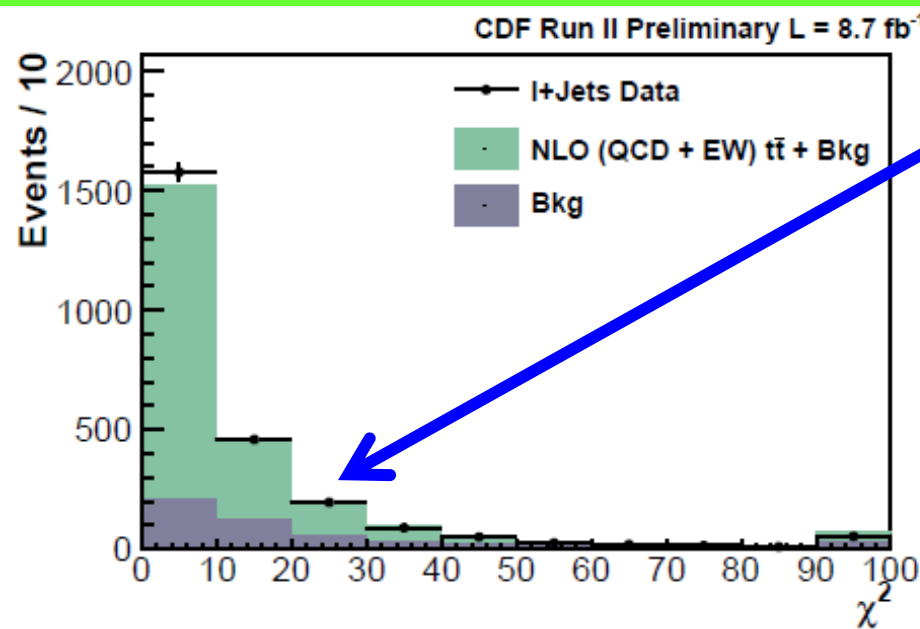
Process	Events
WW	$11.7 \pm 2.4$
WZ	$3.5 \pm 0.6$
ZZ	$2.3 \pm 1.8$
$W\gamma$	$0.4 \pm 0.4$
$DY \rightarrow \tau\tau$	$12.3 \pm 2.2$
$DY \rightarrow ee + \mu\mu$	$22.4 \pm 3.2$
Fakes	$34.3 \pm 14.7$
$t\bar{t}$	$237.1 \pm 11.3$
Total	$324.0 \pm 28.3$
Data	334

Excellent agreement Fairly pure samples

# Reconstructing tops and anti-tops as well as their kinematics

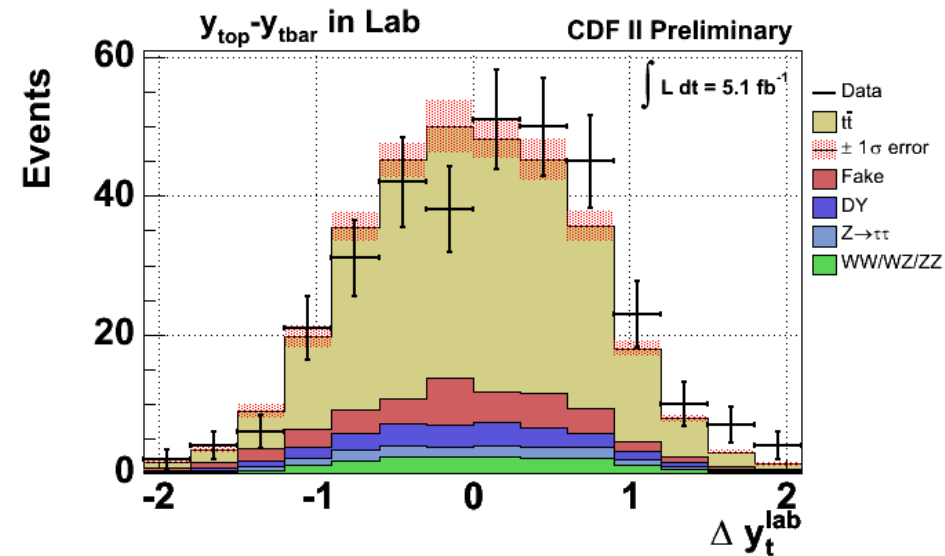
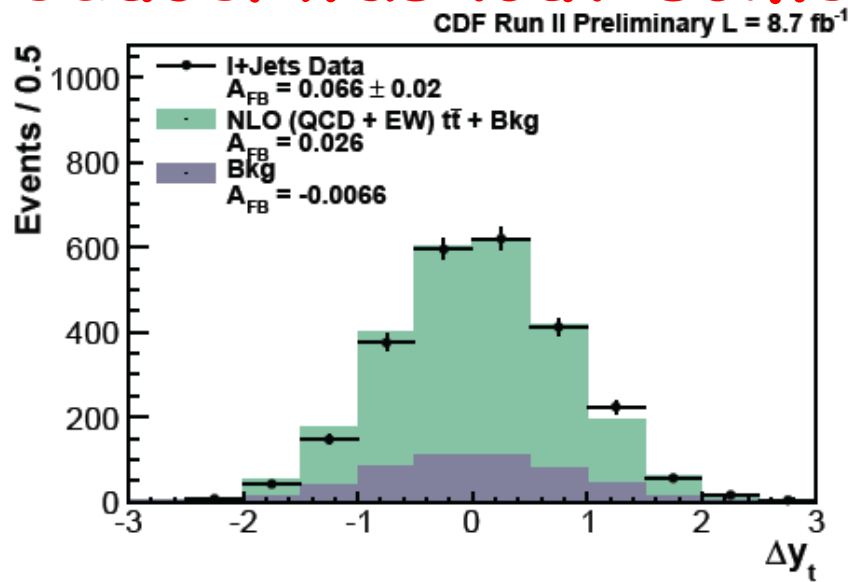
- Reconstruct full  $t\bar{t}$  system kinematics using a fitter
- Constrain to measured  $W$  mass and top masses
- Let reconstructed objects float in fitter within resolution
- Deal with ambiguities by taking best fit of matching to parton level
- Lots of things can go wrong, but this shows that things we can't fix are well understood

Results from Lepton+Jets



# Raw Asymmetry

Detector and measurement effects  
reduce/washout some of the overall asymmetry



## Lepton+Jets

$A_{FB}$  pred = 2.6%

$A_{FB}$  data =  $(6.6 \pm 2)\%$

## Dileptons

N.B: MC for  $t\bar{t}$  prediction  
uses LO only

$A_{FB}$  pred =  $(-2 \pm 2)\%$

$A_{FB}$  data =  $(14 \pm 5)\%$

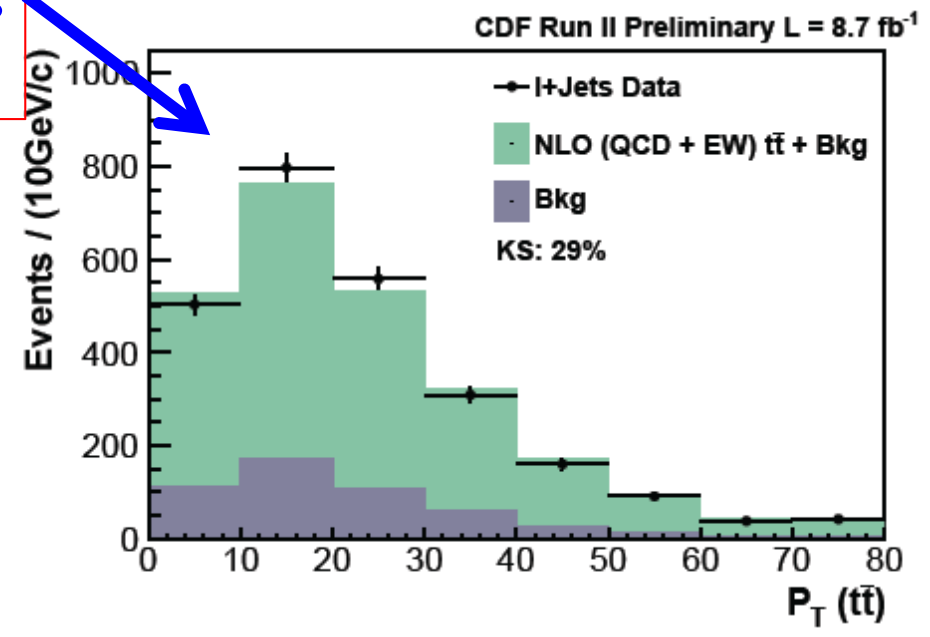
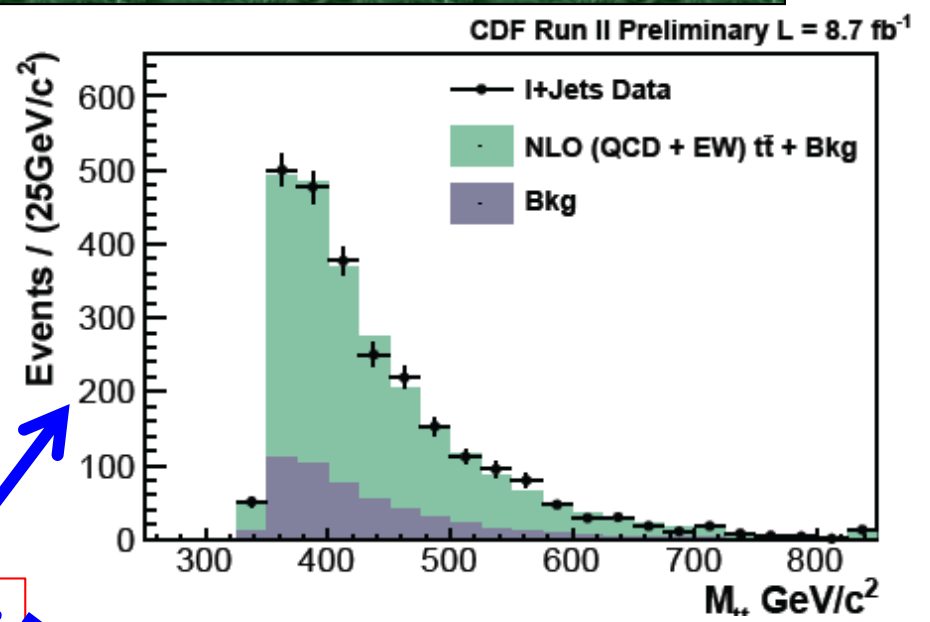
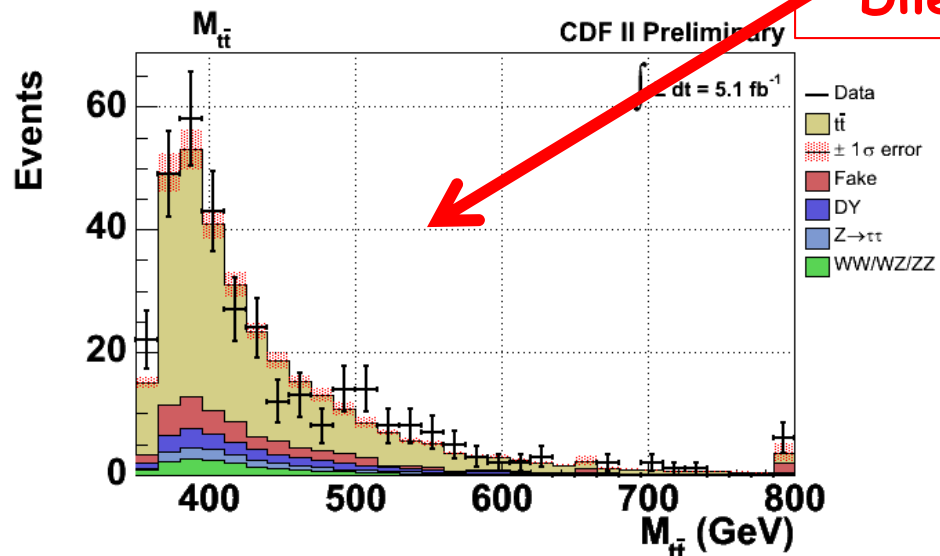
Answers inconsistent with  $A_{FB}=0$  at  $3\sigma$ ,  
also inconsistent with SM

# Problems with the modeling?

If we are going to take this seriously, we need to trust the kinematic modeling

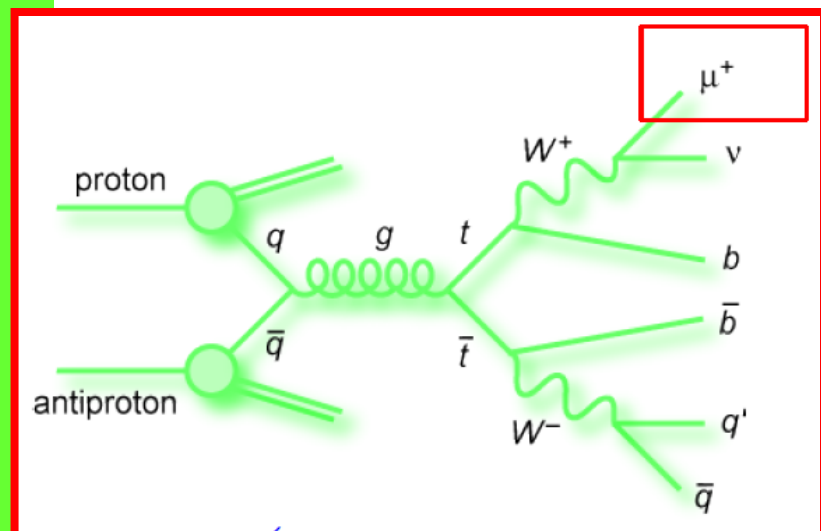
Both the Mass and  $P_T$  of the  $t\bar{t}$  system look well modeled

Lepton+Jets  
Dileptons

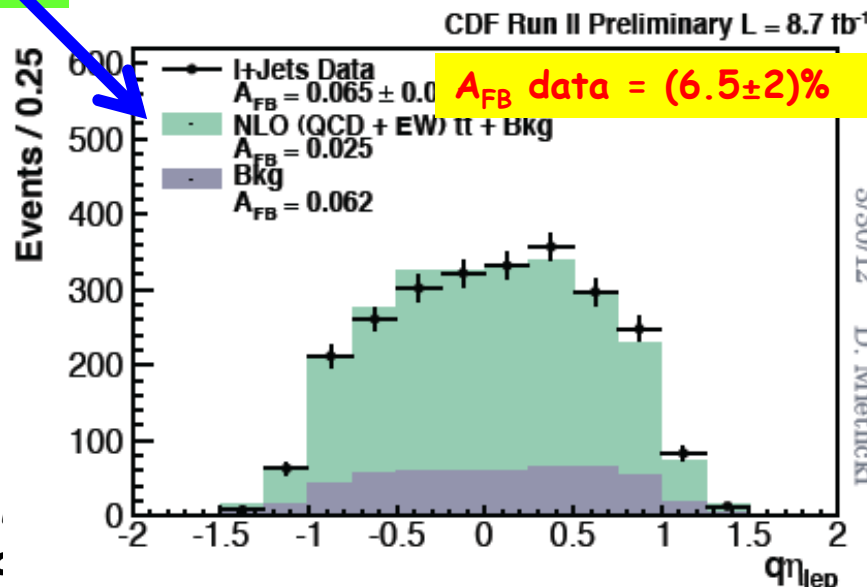
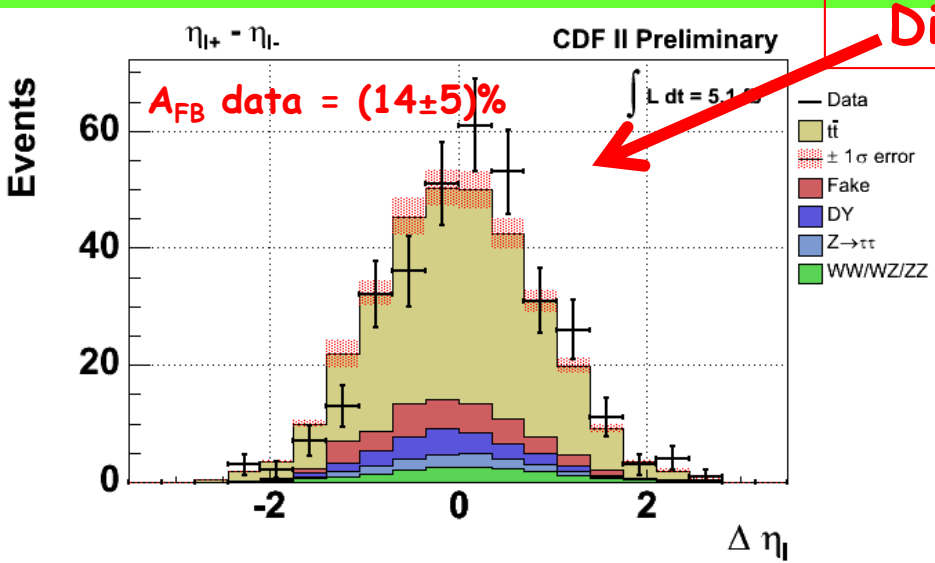


# Independent check: remove the fitting Effect still there using just the lepton $\eta$ and charge?

- Direction of motion of the lepton is correlated with the parent top quark  $\rightarrow$  no reconstruction required
- Isn't really the same as  $A_{FB}$  since it includes spin correlations
- Asymmetry again significantly different from zero



Lepton+Jets  
Dileptons

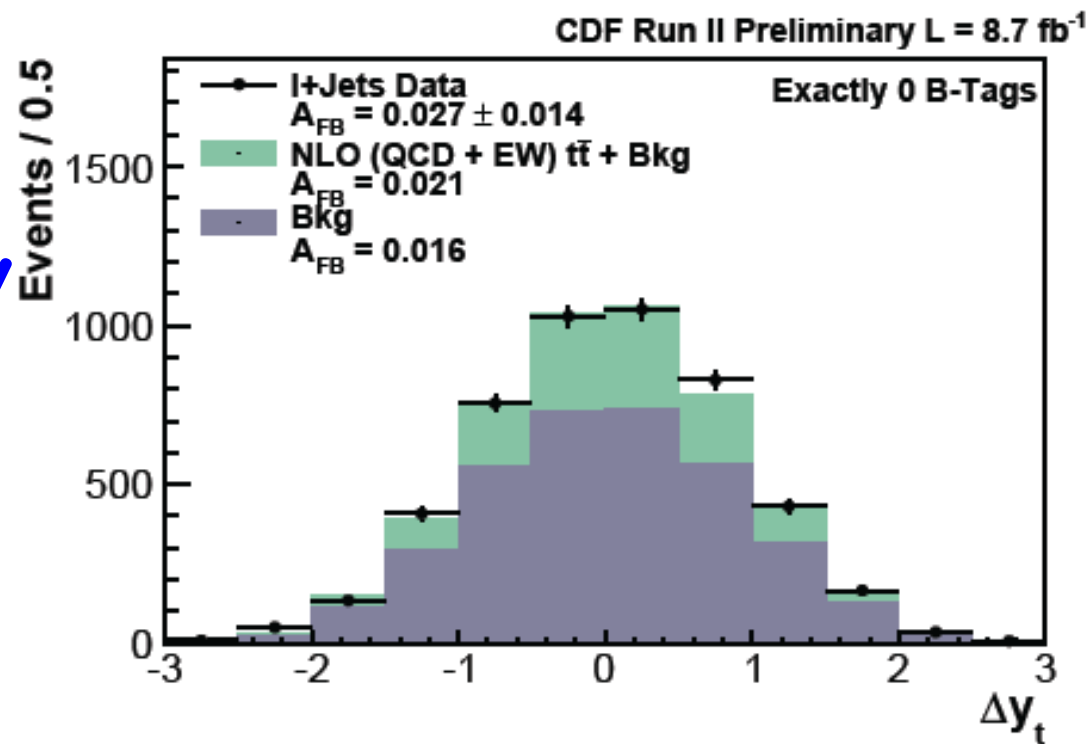


$\sigma_{t\bar{t}}$ , Texas A&M  
 $\sigma_{b\bar{b}}$  in Top Quark

# Check: *Effect still exist in Background Dominated Region?*

## Example in Lepton+Jets

- Same data, but require no  $b$ -tagged jets
- Lots of data, mostly background
- Expect a small asymmetry (2.1%)
- Observe a small asymmetry (2.7%)



# Beyond the Inclusive Raw Measurements:

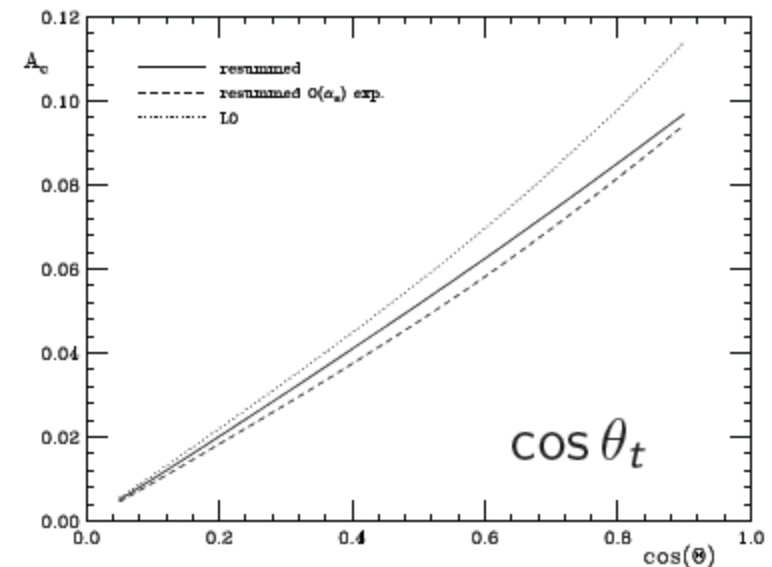
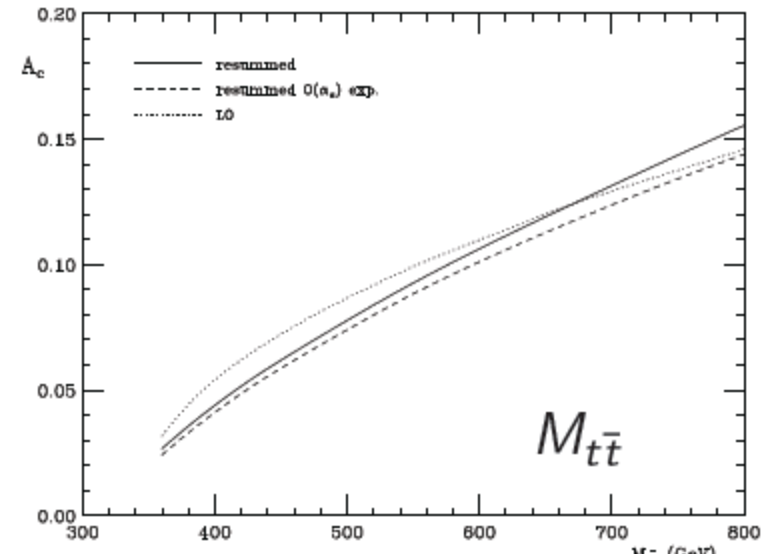
## *Inquiring Minds Want to Know*

### Goals:

- Calculate parton level quantities to compare to theory
- *Does the asymmetry depend on any observables? Should it?*
- *Can we look at these differential asymmetries at parton level?*

# Standard Model Predictions

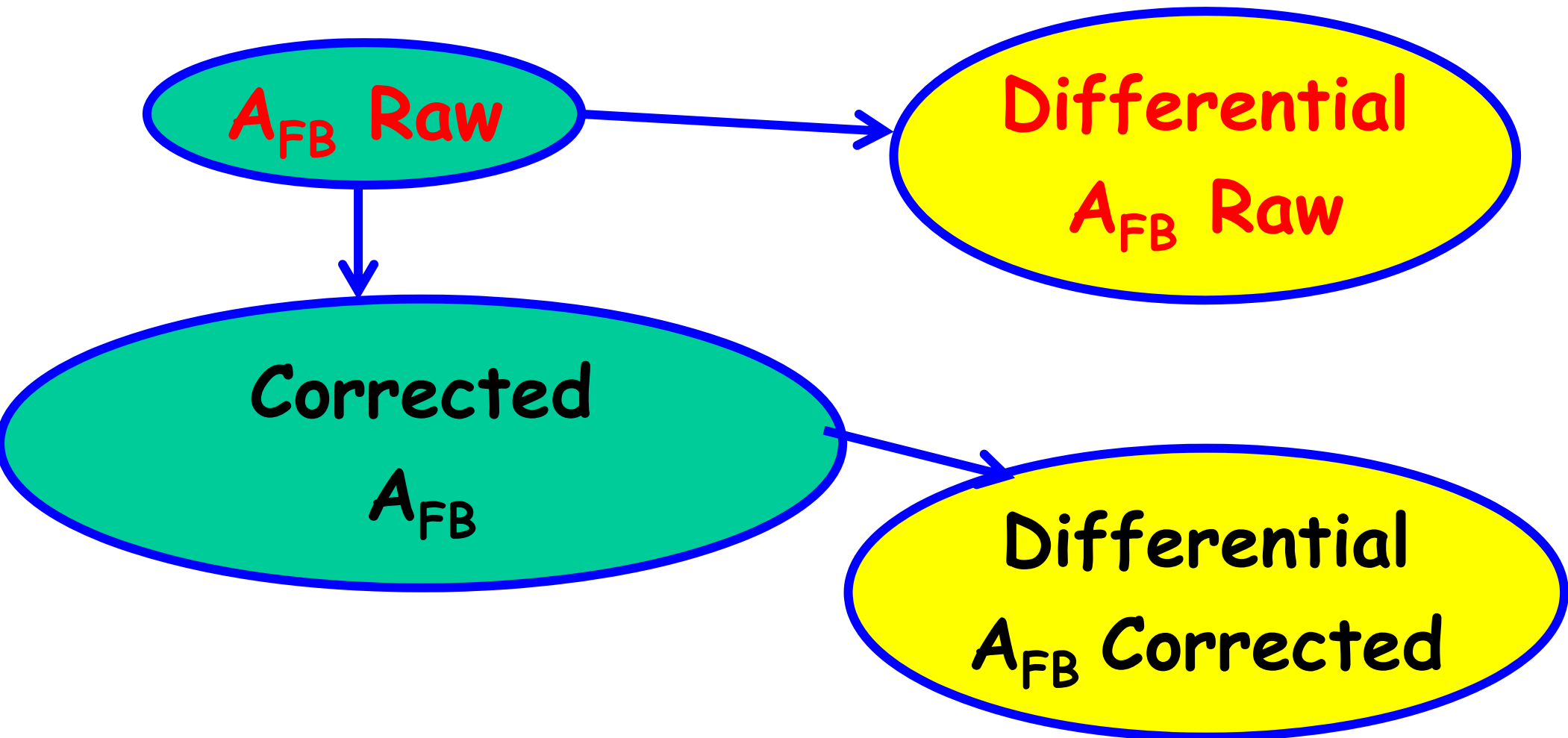
- Asymmetry expected to vary with the mass of the  $t\bar{t}$  system as well as the  $\cos(\theta_t)$ 
  - Again use  $\Delta y$  as our best measure
- Expect an approximately linear dependence



Plots from L. Almeida, G. Sterman and W. Vogelsang  
Phys. Rev. D78, 014008 (2008)

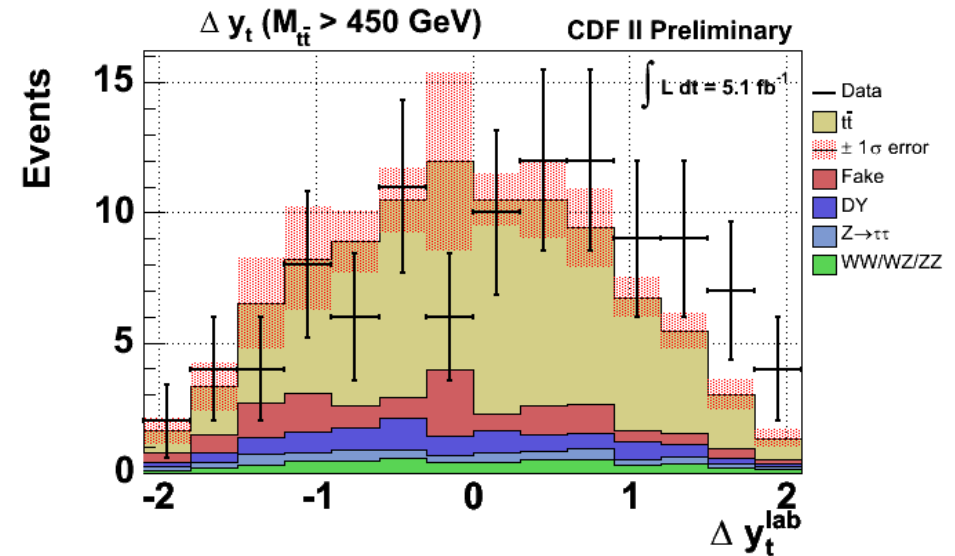
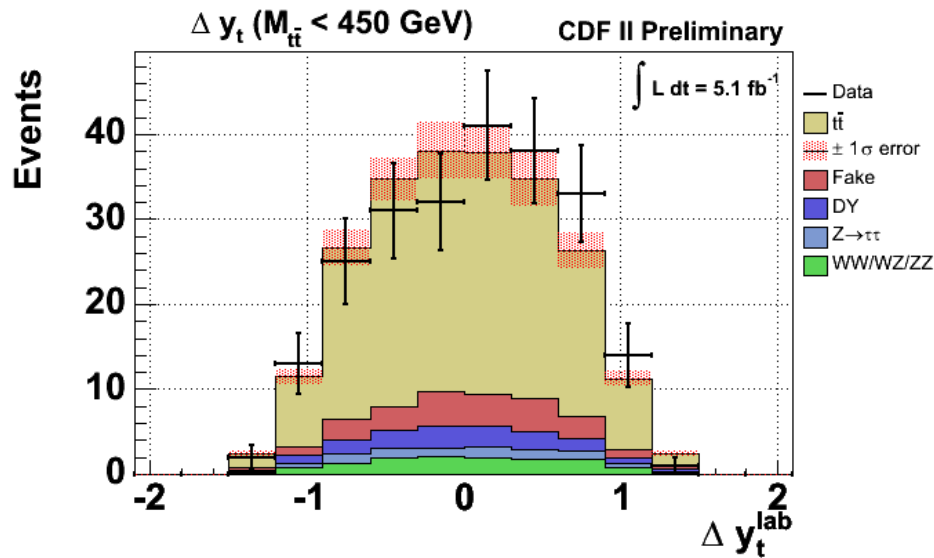


# Let's do 4 separate types of things...



# Dileptons: Asymmetry vs. Mass

- Measure the Asymmetry for low mass and high mass separately
- Small trend upward vs.  $M_{t\bar{t}}$  in dileptons



$M_{t\bar{t}} < 450 \text{ GeV}/c^2$

$A_{\text{FB}} \text{ pred} = (0.3 \pm 3.1)\%$

$A_{\text{FB}} \text{ data} = (10.5 \pm 6.6)\%$

$M_{t\bar{t}} > 450 \text{ GeV}/c^2$

$A_{\text{FB}} \text{ pred} = (-4.0 \pm 5.5)\%$

$A_{\text{FB}} \text{ data} = (12.2 \pm 9.6)\%$

N.B: MC for  $t\bar{t}$  prediction uses LO only

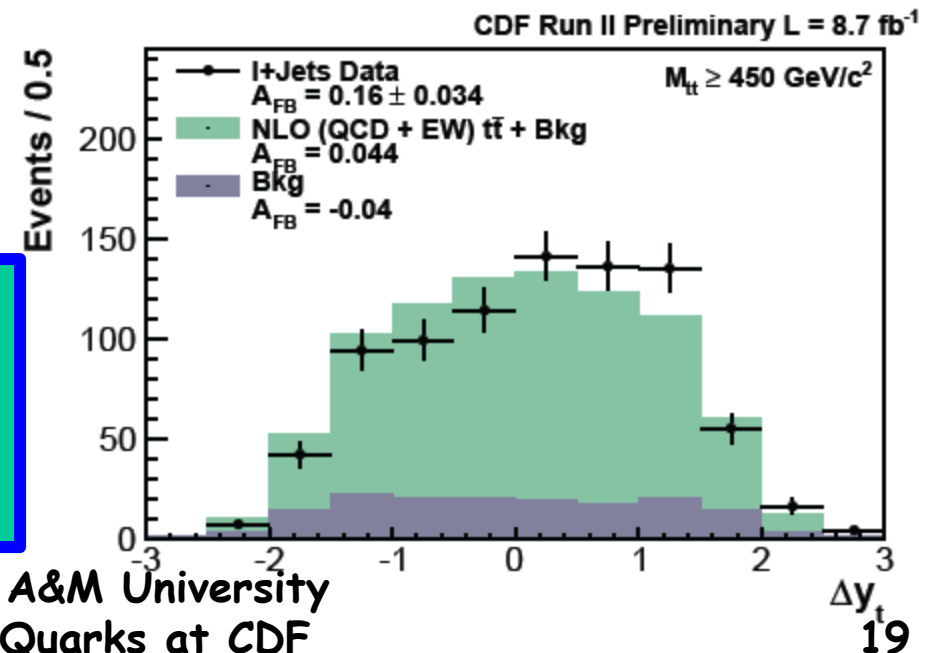
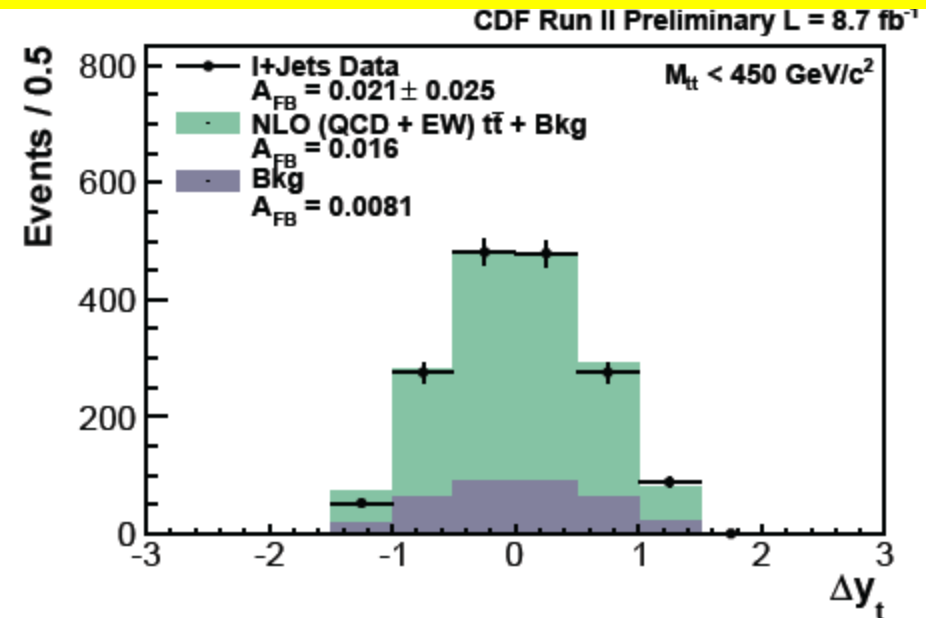
Texas

# Lepton+Jets: Asymmetry vs. Mass

- Observe same trend with higher statistics
- For  $M_{t\bar{t}} < 450 \text{ GeV}/c^2$  asymmetry consistent with zero ( $2.1 \pm 2.5\%$ )
- For  $M_{t\bar{t}} > 450 \text{ GeV}/c^2$  find

$A_{FB}$  Pred = 4.4%

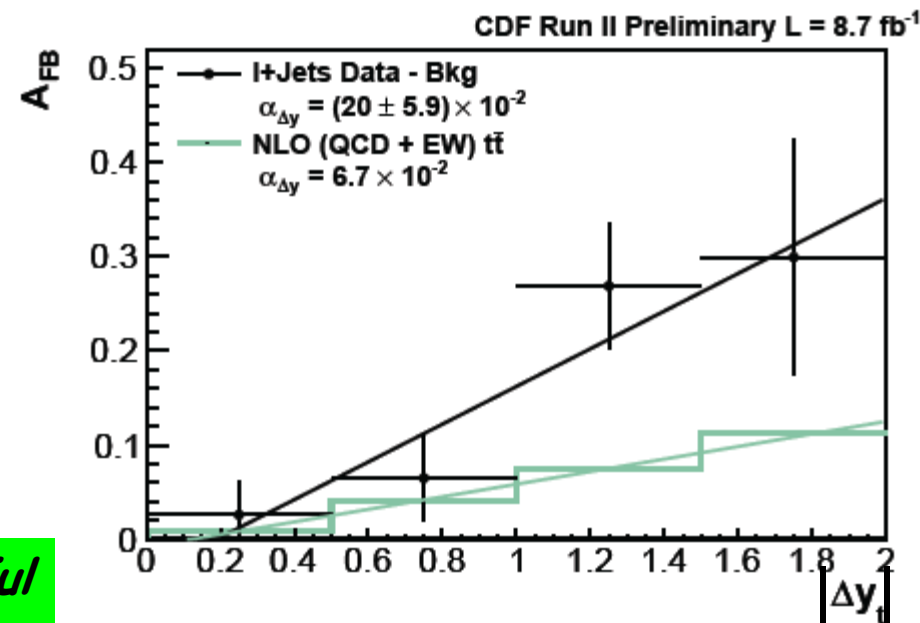
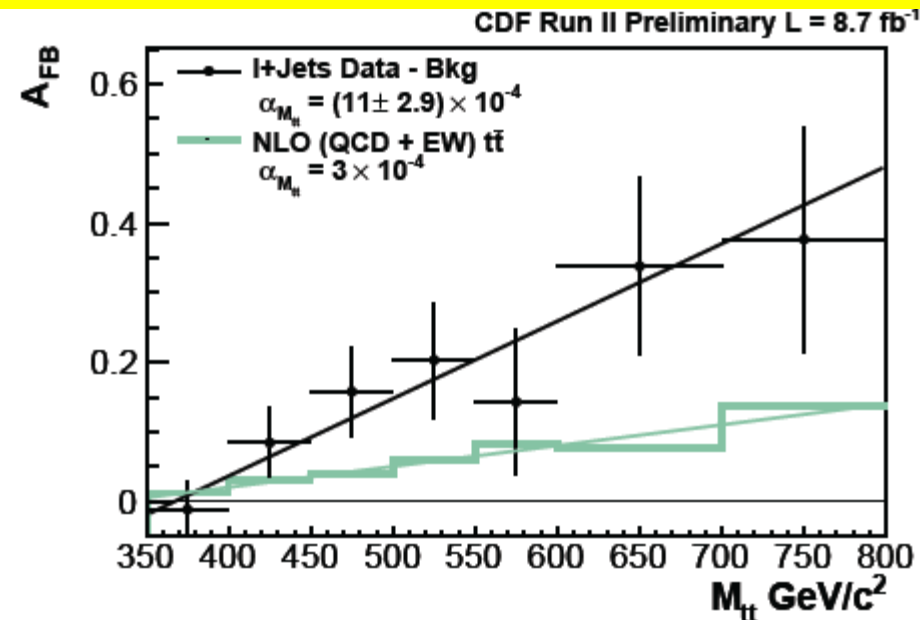
$A_{FB}$  Data =  $(16.0 \pm 3.4)\%$



# Lepton+Jets

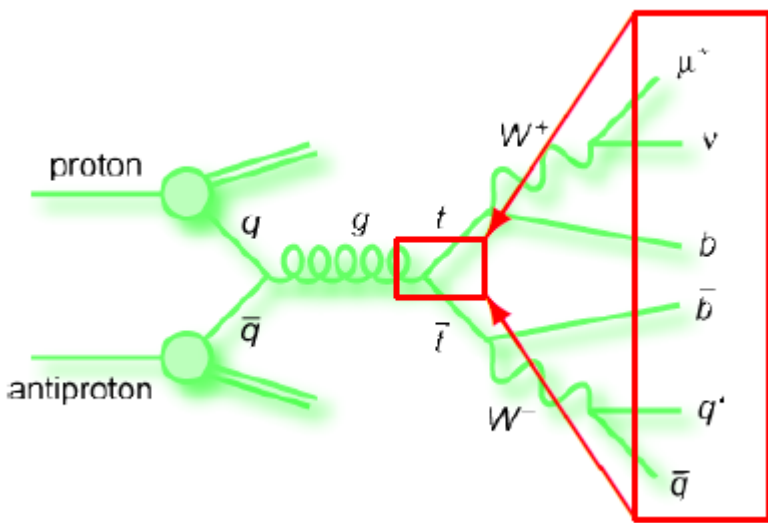
## Asymmetry vs. $M_{t\bar{t}}$ and $|\Delta Y|$

- Can move beyond two bins with full dataset
- Look at the differential  $A_{FB}$  as a function of  $M_{t\bar{t}}$  and  $|\Delta Y|$  after background subtraction
- SM predicts both to be roughly linear
  - Observe a linear dependence in the data
  - Slopes are  $3\sigma$  from zero and inconsistent with SM predicted slopes
  - $p$ -values less than 1% from SM

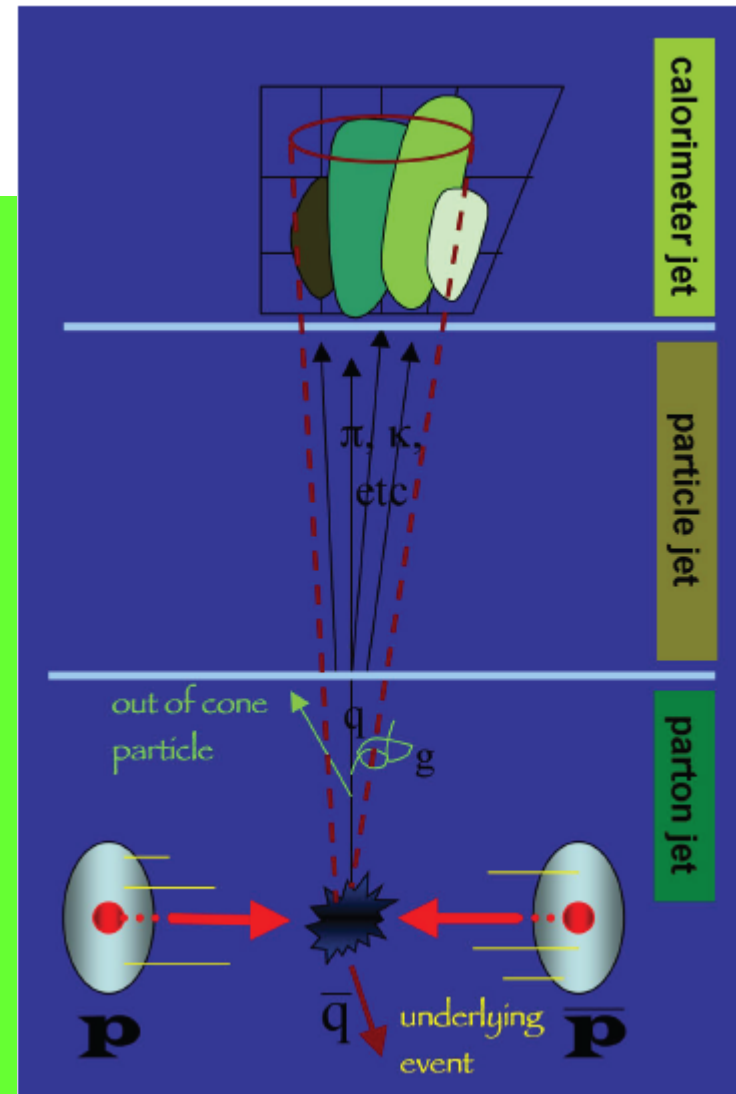


Can the numerical values of these slopes be useful to model builders?

# Working back to Parton Level $A_{FB}$

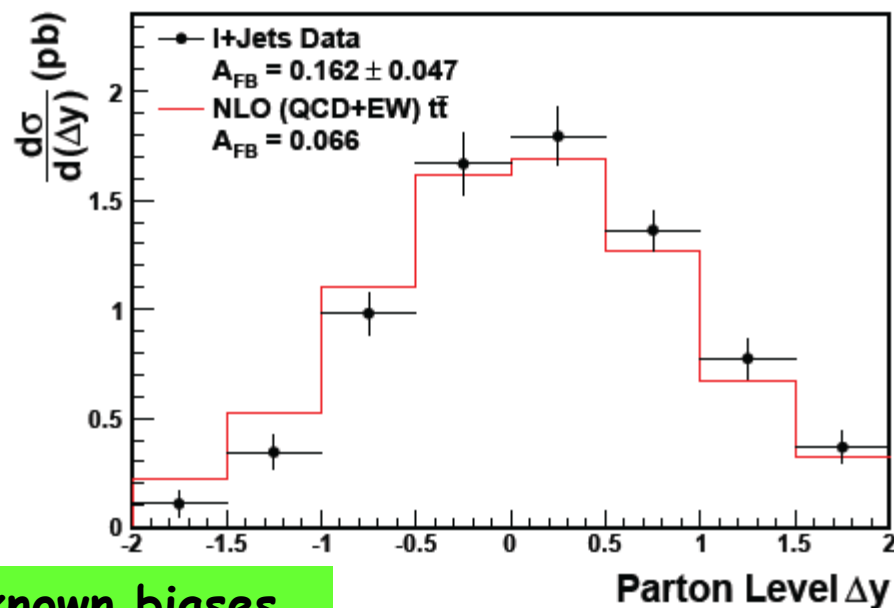
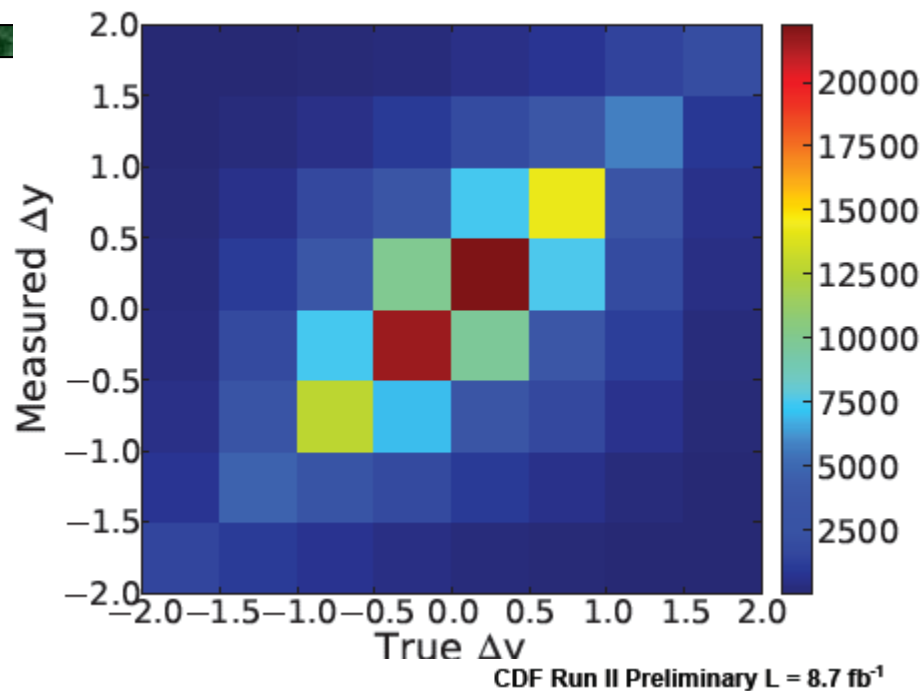


- **Correct for**
  - Finite detector resolution
  - Smearing from incorrect reconstruction
  - Selection Cuts
  - Geometry
  - Trigger
  - Statistics
- **Acceptance correction bin-by-bin of Monte Carlo truth before and after selection**



# A Full Correction Matrix Method

- Use Monte Carlo to estimate detector response functions
- Matrix Methods
- Returns parton level distributions
- Can subtract off backgrounds

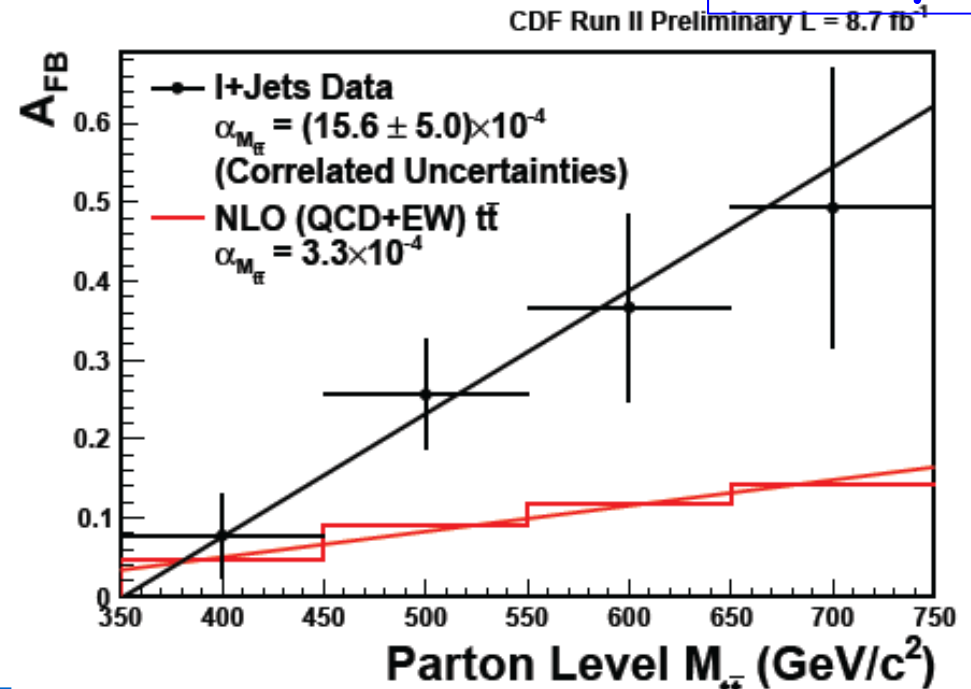
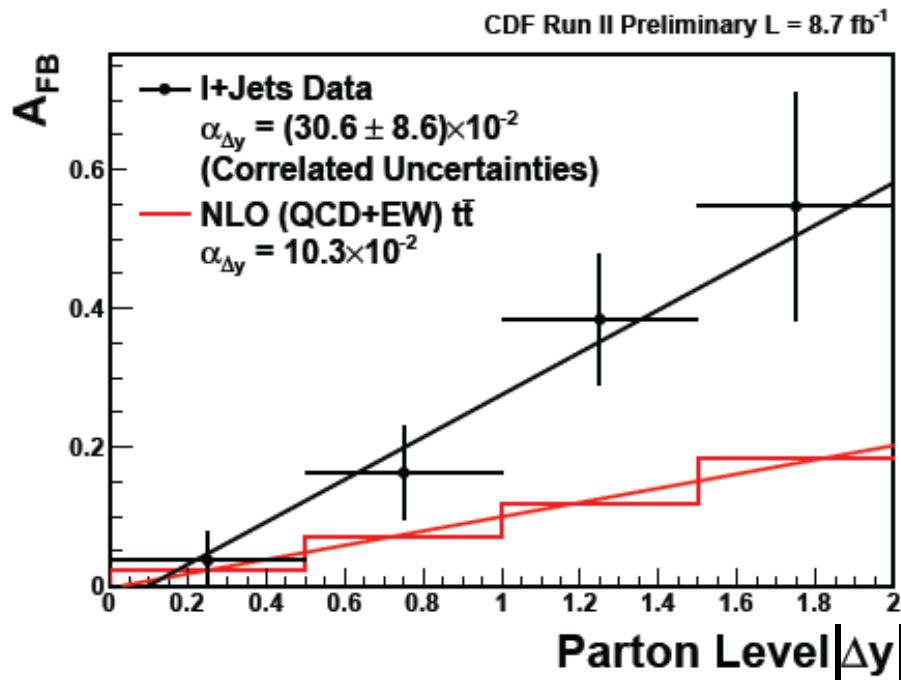


Many potential sources of uncertainty, but no known biases  
Measurement precision dominated by statistical uncertainties

# Parton Level Asymmetries

Differential values of Asymmetry well described by a linear relationship

Lepton+Jets  
only



slope parameter $\alpha$	$A_{FB}$ vs $M_{t\bar{t}}$	$A_{FB}$ vs $\Delta y$
DATA	$(15.6 \pm 5.0) \times 10^{-4}$	$(30.6 \pm 8.6) \times 10^{-2}$
SM	$3.3 \times 10^{-4}$	$10.3 \times 10^{-2}$

Slopes are  $3\sigma$  from zero and inconsistent with SM predicted slopes


# Summary and Conclusions

- Completed two independent studies of  $A_{FB}$  in top quark events using the Lepton+Jets and Dilepton Final states
- Asymmetries often  $3\sigma$  away from zero, and consistently larger than NLO predictions
  - Observed in both datasets
  - Robust against multiple checks of backgrounds and reconstruction procedures
- Both raw and parton-level differential Asymmetries indicate a linear dependence on both  $M_{t\bar{t}}$  and  $|\Delta Y|$
- Have just begin an exciting program ahead of us
  - More studies of Lepton+Jets events
  - Full dataset in Dileptons (add  $b$ -tagging)
  - Collaborating with our friends across the ring, across the oceans and theorists around the world



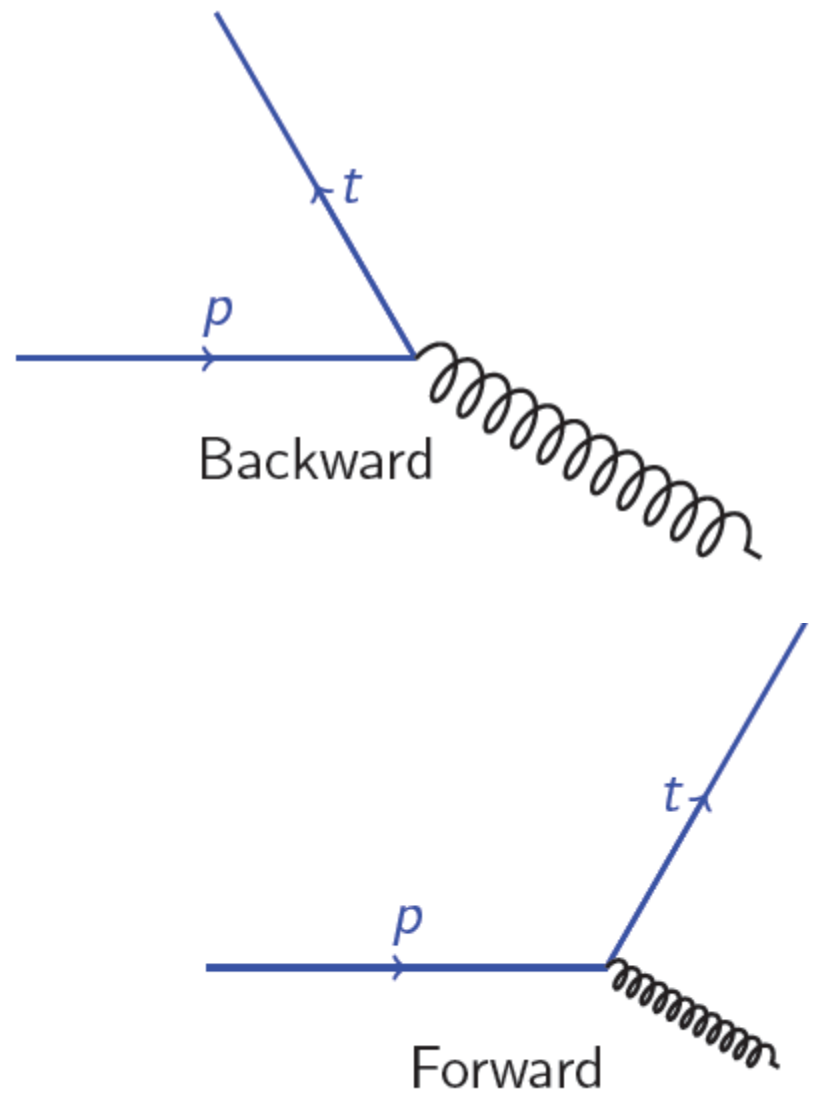


# Backups



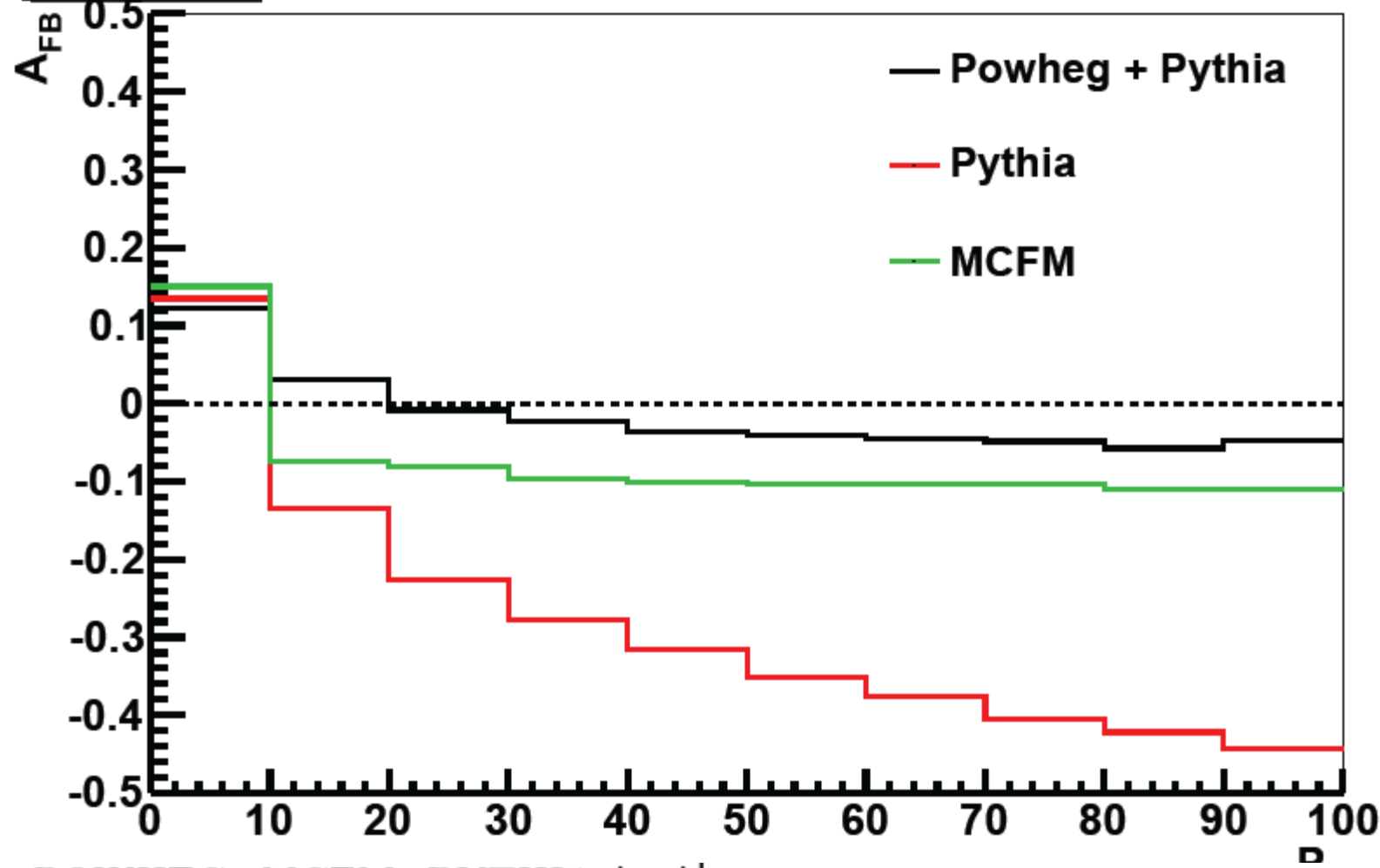
# Backup Slides on $P_T$ of the $t\bar{t}$ System

- Dependence of  $A_{FB}$  on transverse momentum of  $t\bar{t}$  system is very important
- Sensitive to detailed QCD effects
- (Very) rough explanation: In events where top is backwards, color flow from proton to top bends sharply, leading to a “color bremsstrahlung”
- That is, backward events tend to have higher  $t\bar{t} p_T$
- Leads to positive  $A_{FB}$  at low  $p_T$ , negative at high  $p_T$ , even at LO
- Also NLO ISR/FSR interference contributes  $p_T$  dependent  $A_{FB}$



(NOT Feynman diagrams!)

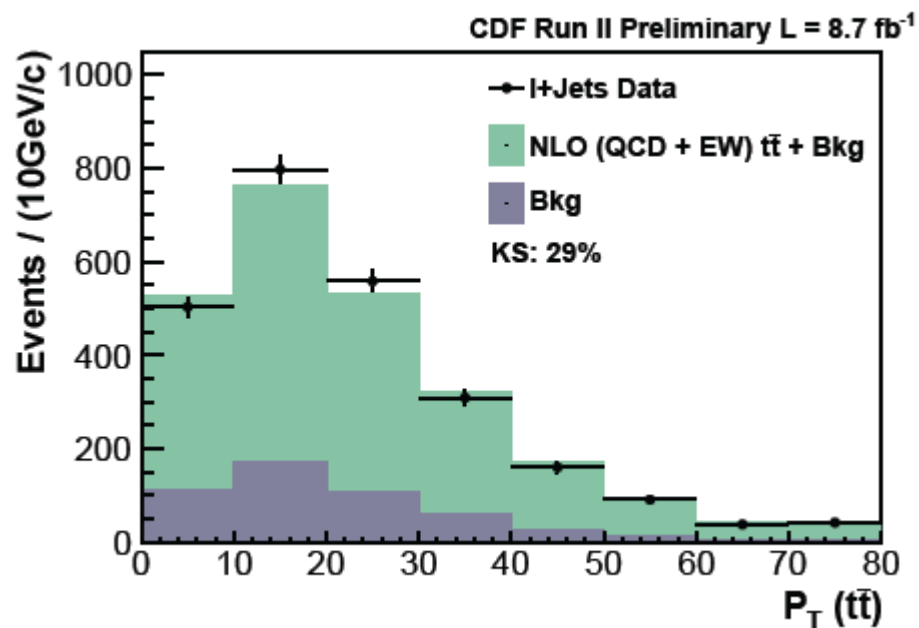
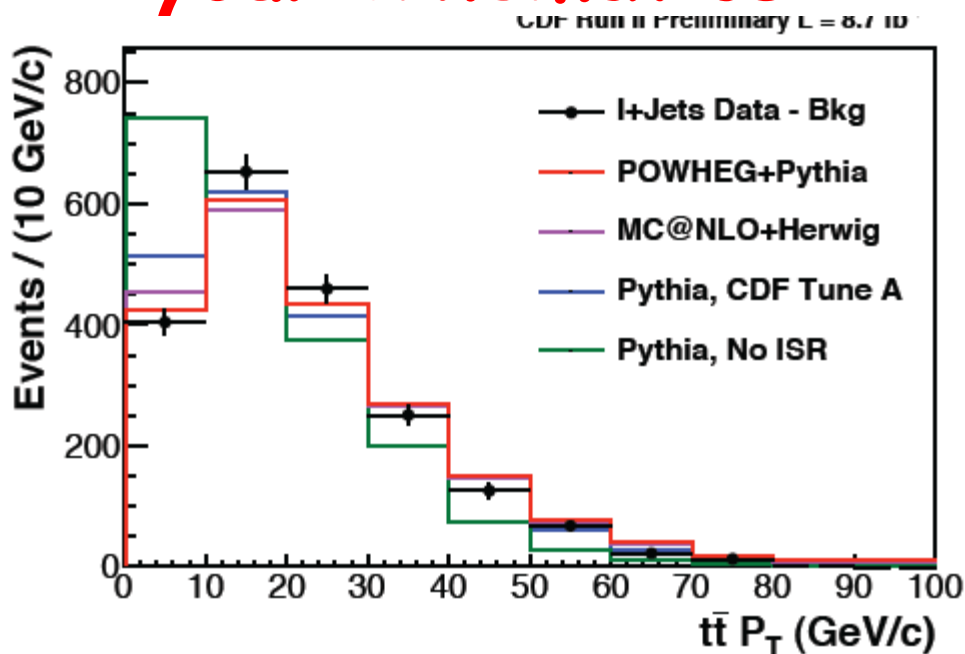
### $A_{FB}$ vs. $P_T$

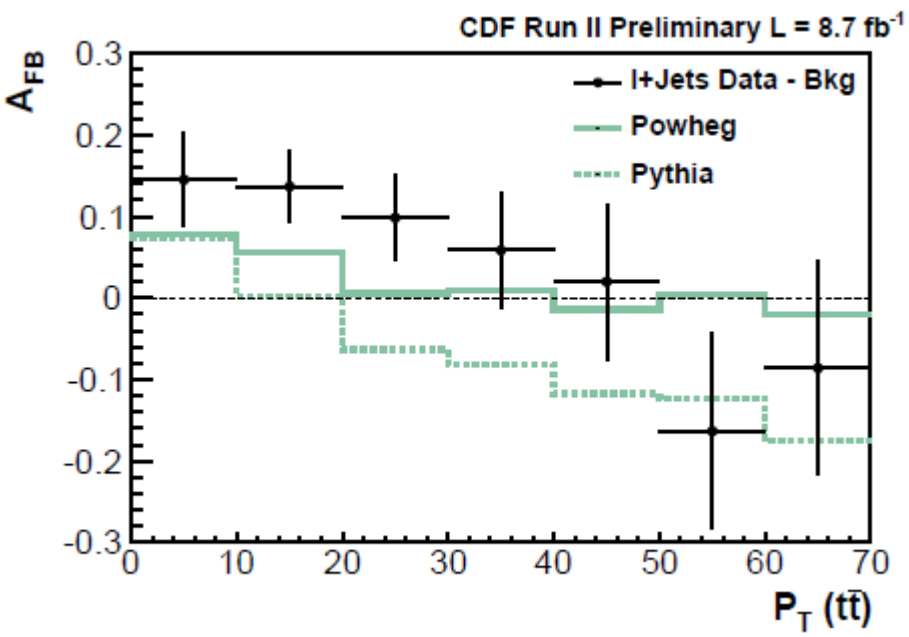


- POWHEG, MCFM, PYTHIA truth
- All same general shape: positive at low  $p_T$ , negative at high  $p_T$

# $P_T$ is important

- Mostly because CDF and Dzero get different results.
- Results clearly depend on which MC you use
- Also must depend on the reconstruction of your kinematics





- Our data (background subtracted) shows a similar dependence on  $p_T$
- Larger overall asymmetry
- Shape compatible with SM predictions from POWHEG and from PYTHIA, total asymmetry not compatible

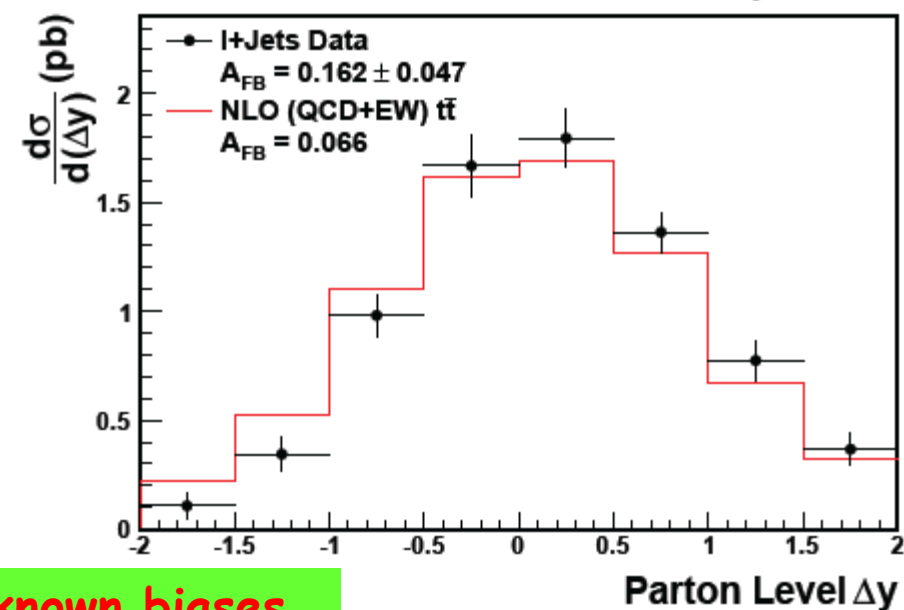
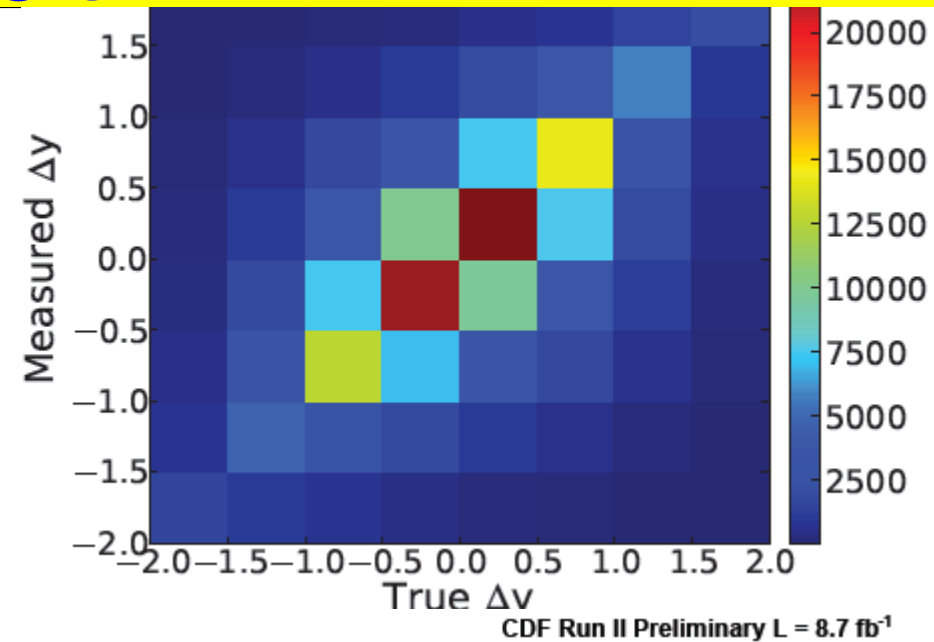


# Backup Slides on the Systematic Uncertainties...

# Small compared to the statistical

# A Full Correction Matrix Method

- Estimate detector response matrix  $S$  from Monte Carlo
- Linear equation for corrected data  $\vec{x}$  from data  $\vec{b}$ :  $S\vec{x} = \vec{b}$
- Inverse problem is ill-conditioned
- Can only be solved in least squares sense ( $\min |S\vec{x} - \vec{b}|^2$ )
- Even then, solution grossly magnifies statistical imprecision
- Use technique from math. stats.: Tikhonov regularization (Höcker and Kartvelishvili 1995)
- Expect true parton level distribution to be smooth



Many potential sources of uncertainty, but no known biases  
 Measurement precision dominated by statistical uncertainties



# Systematics for Lepton+Jets Unfolding

CDF Run II Preliminary  $L = 8.7 \text{ fb}^{-1}$

Source	Systematic Uncertainty
Background Shape	0.014
Background Normalization	0.011
Parton Showering	0.010
Jet Energy Scale	0.005
Initial and Final State Radiation	0.005
Color Reconnection	0.001
Parton Distribution Functions	0.001
Correction Procedure	0.003
Total Systematic Uncertainty	0.022
Statistical Uncertainty	0.041
Total Uncertainty	0.047

# Dilepton Systematics for Corrections

CDF II Preliminary

Source	$\delta A_{\text{true}}$
Background shape	0.043
Detector effect	0.010
Signal MC stat.	0.010
Signal MC	0.018
ISR/FSR uncertainty	0.015
Jet energy scale	0.008
Color reconnection model	0.011
PDF	0.004
Systematics total	0.053
Statistical uncertainty	0.148
Total uncertainty	0.157

## SYSTEMATIC UNCERTAINTIES

- Correction procedure introduces systematic uncertainties related to the signal model, in addition to the background uncertainties discussed previously
  - Total is small compared to the statistical uncertainty

Source	Uncertainty (%)
Background Shape	1.4
Background Normalization	1.1
Parton Showering	1.0
Jet Energy Scale	0.5
Initial/Final State Radiation	0.5
Color Reconnection	0.1
Parton Distribution Functions	0.1
Correction Procedure	0.3
Total Systematic Uncertainty	2.2
Statistical Uncertainty	4.1
Total Uncertainty	4.7



Random Slides I  
didn't use but  
could have

- After DIL event selection, likelihood fitting is applied to reconstruct the direction of  $t$  and  $tbar$  and  $\Delta y_t$

$$\mathcal{L}(\vec{p}_\nu, \vec{p}_{\bar{\nu}}, E_b, E_{\bar{b}}) = P(p_z^{t\bar{t}}) P(p_T^{t\bar{t}}) \frac{1}{\sigma_{\text{jet1}}} \exp\left[-\frac{1}{2} \left\{ \frac{E_{\text{jet1}}^{\text{meas}} - E_{\text{jet1}}^{\text{guess}}}{\sigma_{\text{jet1}}} \right\}^2\right] \times \frac{1}{\sigma_{\text{jet2}}} \exp\left[-\frac{1}{2} \left\{ \frac{E_{\text{jet2}}^{\text{meas}} - E_{\text{jet2}}^{\text{guess}}}{\sigma_{\text{jet2}}} \right\}^2\right] \times \frac{1}{\sigma_x^{\text{MET}}} \exp\left[-\frac{1}{2} \left\{ \frac{E_x^{\text{meas}} - E_x^{\text{guess}}}{\sigma_x^{\text{MET}}} \right\}^2\right] \times \frac{1}{\sigma_y^{\text{MET}}} \exp\left[-\frac{1}{2} \left\{ \frac{E_y^{\text{meas}} - E_y^{\text{guess}}}{\sigma_y^{\text{MET}}} \right\}^2\right],$$

- Resolution functions of JES, MET and probability functions of  $P_T$ ,  $P_z$  are estimated from MC samples

# Checks with Leptons in L+J

- Probably for backups

CDF Run II Preliminary L = 8.7 fb<sup>-1</sup>

Sample	$A_{\text{FB}} (\pm [\text{stat.}+\text{syst.}])$	$A_{\text{FB}} (\pm [\text{stat.}+\text{syst.}])$	$A_{\text{FB}} (\pm [\text{stat.}+\text{syst.}])$
	Inclusive	$M_{t\bar{t}} < 450\text{GeV}/c^2$	$M_{t\bar{t}} \geq 450\text{GeV}/c^2$
All Data	$0.085 \pm 0.025$	$0.025 \pm 0.031$	$0.198 \pm 0.043$
Positive Leptons	$0.100 \pm 0.037$	$0.044 \pm 0.046$	$0.198 \pm 0.060$
Negative Leptons	$0.071 \pm 0.035$	$0.008 \pm 0.043$	$0.198 \pm 0.059$
Exactly 0 <i>b</i> -tags	$0.056 \pm 0.052$	$0.079 \pm 0.066$	$0.005 \pm 0.085$
Exactly 1 <i>b</i> -tags	$0.103 \pm 0.030$	$0.039 \pm 0.037$	$0.226 \pm 0.050$
At least 2 <i>b</i> -tags	$0.034 \pm 0.046$	$-0.014 \pm 0.057$	$0.122 \pm 0.077$
Electron Events	$0.058 \pm 0.038$	$-0.018 \pm 0.048$	$0.199 \pm 0.062$
Muon Events	$0.107 \pm 0.034$	$0.060 \pm 0.041$	$0.197 \pm 0.057$

# Dileptons Summary

CDF II Preliminary

$\Delta y_t$ :

$$A_{\text{obs}} = 0.14 \pm 0.05(\text{stat.})$$

$$A_{\text{sub}} = 0.21 \pm 0.07(\text{stat.}) \pm 0.02(\text{bkg. shape})$$

$$\begin{aligned} A_{\text{true}} &= 0.42 \pm 0.15(\text{stat.}) \pm 0.05(\text{syst.}) \\ &= 0.42 \pm 0.16 \end{aligned}$$

$\Delta \eta_\ell$ :

$$A_{\text{obs}}^{\Delta \eta_\ell} = 0.14 \pm 0.05(\text{stat.})$$

$$A_{\text{sub}}^{\Delta \eta_\ell} = 0.21 \pm 0.07(\text{stat.}) \pm 0.02(\text{bkg. shape})$$